





Robert D. Murchie  
William & Mary  
Virginia  
1809

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A letter from Robert D. Murchie to Mr. Thomas F. Coke in Philadelphia, asking for a position for his nephew, James A. Clark. 10 Dec 1822.  
Memoranda, 1820-1824, some of these being in the form of a diary.

A  
Compendium  
of  
Lectures  
as delivered by  
James Madison  
President  
of  
William & Mary

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# Natural Philosophy

## Lecture 1<sup>st</sup> introductory

What is meant by the word phenomenon?

It signifies an appearance, or in a more enlarged acceptation, whatever is perceived by our senses. Thus the fall of a stone, evaporation of water, a flash of lightning &c. are all phenomena.

On what do all phenomena depend?

On properties peculiar to different bodies. For instance, it is the property of a stone to fall towards the earth, of water to be evaporable &c.

What is the design of natural philosophy?

To become acquainted with the properties of natural bodies, investigate their causes, and thence to infer useful deductions. Thus the properties of the air we breathe, the action and power of our limbs, the light, the sound, and other perceptions of our senses, the actions of engines; the vicissitudes of the seasons, the movements of the celestial bodies, &c. do all fall under the consideration of the philosopher.

Are the axioms of philosophy as evident as those of geometry?

No, they only assert things which have been constantly shown and confirmed by experience, are not contradicted either by reason or experiment, but they are not absolutely certain.

Illustrate the third axiom.

Some persons may perhaps be inclined to doubt the propriety of this axiom, seeing that a great many things appear to be utterly destroyed by the action of fire, also that water may be caused to disappear by means of evaporation, &c. But it must be observed that in these cases the substances are not annihilated, but are only dispersed, or removed from one place to another, or they are divided into particles so minute as to elude our senses. For instance if a piece of

wood be placed on the fire, it will in a short time be reduced to a heap of ashes, which does not exceed the one hundredth part of the weight & bulk of the original piece of wood; although in this case, an apparent annihilation takes place, yet the wood is only separated into its component parts. The fluid part becomes steam, the light coaly part either adheres to the chimney or is dispersed through the air, and in fine, if after the combustion all these parts were collected (which can in a great measure be done) the result of all their weights taken together would equal the weight of the original body.

Why have the rules of philosophizing been formed? To prevent errors as much as possible, and to facilitate the progress of the student in acquiring true and useful knowledge.

What degree of evidence should be annexed to natural philosophy? Physical matters are not capable of such absolute certainty as the branches of mathematics. We can only say in natural philosophy, that because some particular effects have been constantly produced under certain circumstances; therefore that they will continue to be produced as long as the same circumstances exist; and likewise that they do, most probably, depend upon those circumstances.

What is time? It is incapable of proper definition. All that can be said in regard to it is, that it is divided into absolute and relative. Absolute time flows equably but does not refer to the motion of bodies. Relative time is that portion of absolute time during which a certain movement is performed, and when they are equably and steadily performed we assume some of those movements as the measures of time. For instance, the apparent movement of the sun round the earth we call a day. The 24<sup>th</sup> part of that day, we have

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What are the laws of nature?

They are those immutable laws by which every phenomenon in nature is regulated, and which preserve uniformity and order throughout the stupendous system of materialism.

What is the method which the rules of philosophizing point out for our enquiries into the laws of nature?

Instead of forming vain hypotheses, the philosopher should first collect a history of facts, observe the laws by which, under the same circumstances, they are always governed, and thence deduce the causes of these effects.

What are the inducements to study natural philosophy?

They are very great and very numerous, & drawn principally from five sources. 1.<sup>st</sup> Its extensive utility. 2.<sup>nd</sup> The gratification which the mind feels in pursuit of it. 3.<sup>rd</sup> The novelty and grandeur of the subject. 4.<sup>th</sup> It is the best field for exercising the human intellect. 5.<sup>th</sup> It is the source of the sublimest conceptions of the author of the universe.

First from its extensive utility. The science of mechanics alone, by the invention of machines which abridge human labour, has rendered infinite service to society. By this science mankind have been able to erect superb edifices, and when assisted by the discoveries of philosophy in the science of magnetism, to build vessels, and equip them as it were, with a soul, which should direct their course over boundless tracts of water in order to convey to one nation the necessaries and luxuries of others the most remote, and in order to keep up that mutual communication between the different quarters of the globe, so essential to human knowledge as well as happiness. Secondly the human mind is so constituted as to receive pleasure from a variety of objects and sources, but as these are principally to be found in the works



of nature, a mind employed in the study of philosophy, whose object is nature, must necessarily receive great additional inducements from the source to study this science, especially as, thirdly, something new or grand is constantly presenting itself in the course of this study. Fourthly, the mind of man finds ample room to exert and display its faculties, in a field to which imagination itself can set no bounds. After contemplation, all inferior things, and observing the wonderful adaptation of means to ends, the mind disdaineth to be confined to this terrestrial scene, springs aloft into the ethereal regions of unbounded space, and while it contemplates the infinite wisdom and power to form so many suns and systems of worlds, and to adjust their bulks, orbits, and periods with such exactness, is led to form the sublimest conceptions of the author of the universe. The mind becomes expanded and enlarged in viewing the astonishing wisdom and ingenuity displayed in the mechanism of such immense systems of being in the contemplation of which it is itself overwhelmed and swallowed up.

What the general view of the progress of this science together with the causes which so long retarded that progress?

Man being surrounded by a variety of objects and inhabiting a world whose innumerable new appearances were constantly presenting themselves to his view; the natural curiosity of his mind must from the earliest ages have drawn his attention to them and led him to enquire into their causes; but having nothing to direct him in his researches, and being unacquainted with the wisdom and ingenuity displayed in the works of nature, he wandered about in the mazes of uncertainty, and had recourse at last to his own imagination to invent

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a system by which he might account for the appearances which presented themselves. But this could be nothing more than a system of conjecture without proof to support it, and could challenge the belief of none but the author, whose reason was fogged in the warmth of his imagination, because no improvement being hitherto made in the method of recording events, no history of phenomena had been yet collected, & there could be no foundation upon which to erect a superstructure. To undermine its shallow foundation would therefore be no difficult task & would be immediately attempted by those who envied of his false wisdom to raise their own on its ruins. But the foundation of this second being not more solid than the former, it too in its turn became unable to withstand the test of examination. Thus was one hypothesis raised on the ruins of another which in its turn gave way to a succeeding one, for many thousand years without arriving any nearer the truth. A luxury, concurrence of fortunate events contributed however gradually to elevate man from this degraded state, and to give to his view those secret principles which had been long concealed in the womb of nature. The principal of these events were 1<sup>st</sup> the invention or improvement of the mariner's compass in the year 1302 by means of which commerce has been extended over the globe and knowledge disseminated through every class of men. On this discovery gradually brought to light another. The extension of navigation consequent on the discovery of the compass enabled every individual to avail himself in some measure of the discoveries and improvements made in every other country even the most distant. About the year 1430 the art of printing was invented. The union of these two very important inventions began to form all the

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nations of the earth into one formidable republic  
of science. From this time an amelioration of  
the condition of the human species began to take  
place and the human mind was roused from  
that state of lethargy in which it had remained  
for many ages. Philosophers began to arise who turned  
their attention to the works of nature that nobler  
field of improvement to man, which had been  
totally neglected during the long reigns of ignorance  
and superstition. About the year 1608 Galileo  
a citizen of Florence introduced the telescope  
into use which had been just invented in Holland,  
by means of which he discovered the satellites of  
Saturn. But Sir Francis Bacon was the  
first who pointed out the proper method to be  
pursued in philosophical researches in a  
collegiate exercise at the age of 16. This method  
was afterwards pursued by Mr. Boyle who made  
many important experiments and discoveries.  
But it was Sir Isaac Newton who first discovered  
the general law of nature namely, gravity,  
which operates throughout the universe, keeps the  
planets in their orbits, and preserves the whole  
fabric of nature from confusion and disorder.  
He laid the foundation of the present system of  
philosophy which has finally overthrown the  
chimerical hypothesis which so long retarded  
the progress of the true philosophy. The bare  
mention of the names of these illustrious heroes  
of science who have since turned their attention  
to the cultivation of philosophy, would be  
too tedious a task to attempt.

What are the qualities necessary for a student who  
would profit by this course?

He should endeavour to divest himself as much  
as possible of every kind of prejudice. He should  
take nothing for granted that is not satisfactorily

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proved, but enter with spirit in the consideration  
of whatever is offered, and examine it with the  
strictest attention, and utmost impartiality.  
Unremitted attendance & diligent application are  
always necessary for those who wish to make any  
progress in science.



infinite is absurd, because it consists of parts. Divisibility is the property by which all matter may be divided into parts. It evidently exists, because the particles of bodies are all distinct and never can exist in the same place. Attraction is the property by which one body tends to, or endeavours to approach another. Figurability is the property by which matter is capable of an infinite variety of shapes. It arises from this, that matter is not infinite and must therefore be circumscribed by limits which constitute the figure. It consists in the interstice between the particles of matter, which are found in all bodies.

What are the experiments to prove the solidity of bodies apparently the least solid?

Take a glass tube open at one end only, immerse the open end into water & you will find that the included air will not suffer the water to rise in the tube which it would do were the other end of the tube open. Therefore air is solid according to the definition of solidity.

Is matter infinitely divisible?

That matter is infinitely divisible may be demonstrated mathematically, but when we come to apply this principle to actual experiment, we shall find that the powers of man have not arrived at that degree of perfection to be capable of carrying on the division to such an extent.

Is the mathematical demonstration applicable to the material world?

Is it not on account of the imperfection of the powers of man, which prevents him carrying on the division to such an extent.

General properties of matter are the following, Extension, Solidity, Intractability (or vis inertiae), Divisibility, and Attractibility; to which have been added, Configurability, Inertia, Rarefactibility, Condensibility, Compressibility, and Elasticity. Rarefactibility is that property of bodies by which they become inflated or expanded by heat. Condensibility is the reverse of rarefactibility, being that property

which bodies have to become warped or contracted by cold. Compressibility is the property whereby bodies are capable of being brought into a smaller compass. Elasticity is that tendency which all bodies have whenever compressed or extended to recapture their former state. To prove the solidity of water is not (which of all bodies appears the least) to fill a bladder with air or water, and the sides cannot be brought into contact. Some have denied that matter is infinitely divisible, but let them consider, that if the smallest particle of matter be placed on a smooth surface, some part of it will be farther from the surface than another. But that matter, if not infinitely divisible, is at least indeterminately so, may be proved by mathematical demonstration.



With respect to divisibility, there are two remarkable instances which deserve to be mentioned. A single grain of gold may be beat out into a leaf containing 50 square inches which may be divided into 500,000 parts visible to the naked eye. These again, by a Telescope magnifying only ten times, may be divided so as to make the 50 millionth part visible. But nature goes still farther than art; for we are told by P. N. Leuwenhoek that there are more animals in the milk of a single Cod fish, than there are inhabitants on the earth; and comparing these with grains of common sand, by means of a microscope, it appears that a single grain is larger than a millions of them. The porosity of bodies is manifest by the following experiment. Exhaust the air from a receiver which has a piece of wood on top; on this pour Mercury and it will pass thro' the pores of the wood. To this is also owing the easy transmission of light thro' glass. It was shown by Des Cartes, and his followers that a vacuum could not exist in nature. But the Platonic argument completely

refers than body; for of all the infinite variety of forms which  
 matter can assume, Nature provides that there were only five  
 which could be so placed as to leave no Interstices or vacu-  
 ities between them: hence the apostles of a phisic were oblig'd  
 to prove, that though matter is liable to numberless different  
 forms, yet all its particles must have some one of the five  
 following, Tetrahedron, Hexahedron, Octohedron, Dodecahedron,  
 and Spherohedron, which are call'd the Platonic bodies; for  
 if the particles assumed any other form whatsoever, it is very  
 evident that they admit vacancies in the composition of any  
 body. Since the invention of the air pump, the error of Des Cartes  
 has been plainly shewn; for a quince and a feather will  
 fall to the bottom of an exhausted receiver in the same time.  
 The Cartesians contended that there was a certain subtle fluid,  
 which would penetrate the hardest bodies, by which all space  
 was fill'd up. The ancients supposed Fire, Earth, Air and  
 Water to be the elements or primary principles of all bodies.  
 It is true they are found in all bodies whatever: yet the Chemists  
 of modern times have discovered that they are not in a  
 simple state. Water has been decompos'd, and found to consist  
 of two different kinds of Gas. It is concluded by the moderns,  
 that to discover the elements of bodies, is beyond the capacity  
 of man, and they have with more reason class'd them under  
 different heads according to their most distinguishing and  
 striking properties, as Watery, Earthy, Inflammable, Saline &  
 Metallic. Attraction and Repulsion are among the general  
 properties of bodies, being that tendency which they have to  
 approach, or the power to recede from each other: yet in using these  
 terms, they are not to be consider'd as the physical cause, but  
 only as the effect of some unknown cause. There are several  
 different kinds of attraction, as that of Cohesion, of Gravi-  
 tation, of Adhesion, of Electricity, and Elective force attractions.  
 The first is that which takes place between the minute  
 particles of bodies. Attraction of gravitation is that power  
 by which distant bodies tend towards each other: That of  
 Magnetism, is the peculiar attraction which the loadstone  
 has for iron and all feruginous substances.



Attraction of Electricity, is that which several bodies, as Amber, Wax, Glass &c. exhibit when heated by rubbing. Elective attraction is when a menstruum dissolves some bodies in preference to others. There are three laws belonging to attraction of cohesion. 1<sup>st</sup> It takes place only at a small distance, and between the smallest particles of bodies. 2<sup>nd</sup> It is in proportion to the quantity of surface. 3<sup>rd</sup> It is mutual and common between all bodies. The simplest instances of water, or two globules of mercury. It is by this attraction that several phenomena are accounted for, as the ascent of sap in trees, the rise of nutritive juice, or the moisture of the earth, in plants, & the stems of flowers, the rise of water in capillary tubes above the external surface, the water being attracted by the annule of the tube. Upon this principle depends the rationale of cements & solderings &c. for the surfaces being brought into contact, the attraction of cohesion immediately takes place. By this attraction we account for hardness, softness, fluidity, fermentation &c. When the particles are flat the body is hard, when they touch in few or points & are more round, they are soft, when spherical or nearly so, they form a fluid. Fermentation too, is produced by this attraction, as it consists in an internal agitation arising from the mutual action & attraction of the particles. As to Elasticity, the real cause is not yet known. In all cases the attraction of cohesion is destroyed by separating the parts at a very small distance.

The height of water rising in capillary tubes will be inversely as their diameters.

# Lecture 3<sup>rd</sup> Chemical Affinity.

On the general laws which tend to bring the particles of bodies together, and to maintain them in a state of combination.

Were it not for this force which Chemists call affinity, there would be no such thing as solidity. It is the agent employed by nature to maintain its equilibrium by forming a balance to the power of repulsion, or that extremity, which is called caloric, which is ever tending to divide the particles of bodies. Water affords the simplest instance of existence. Place two drops near each other, & they will mutually approach & form one globule. Two polished surfaces when brought into contact afford another instance. They will cohere so very strongly, as to require considerable force or weight to separate them. This affinity is exerted between particles of the same nature, & also between those of a different nature. That species of attraction which exists between the minute particles of bodies, has been called affinity, 1<sup>st</sup>. Because Chemists supposed it depended on a certain analogy, or conformity in the principles of those bodies between which it existed. 2<sup>dly</sup>, to distinguish it from the planetary attraction discovered by Newton, of which it appears to be a modification. Hence it is considered in a twofold view. First, that which exists between bodies of a similar nature, or affinity of aggregation. In this attraction the real properties of bodies cannot be changed, for if water be united with water, the union must still remain water. But it must be distinguished from both a mixture & a heap; for, the an heap consists of similar parts, these parts are disposed to unity & without adhesion. A mixture is composed of particles of a different nature, united incoherently. An heap may become an aggregate by fusion & cooling, thus; melt the flowers of sulphur, and while they are in a state of liquification, this attraction will act, and render them when cool a complete

aggregate. The affinity of aggregation exists in different degrees, & is measured by the force requisite to separate the integral parts of the aggregate body. Aggregates are distinguished into four kinds, 1.<sup>st</sup> the hard or solid aggregate, whose parts are so forcibly united that a considerable effort is necessary to separate them. 2.<sup>nd</sup> The soft aggregate whose constituent parts may be made to change their relative situations without separation. 3.<sup>rd</sup> the airiform aggregate, whose parts are so small & subtil as to escape the eye. The atmosphere affords an example of it. 4.<sup>th</sup> The fluid aggregate, whose integral parts are separated by the slightest efforts. Water presents us with an instance of each of the four kinds. When frozen, it forms the hard, or solid aggregate, when muddy, or in a state between the solid & fluid, it forms the soft. In the common state, it is the fluid, and when its parts are disengaged by a large quantity of caloric, it exhibits an example of the airiform aggregate. Thus we see that the four kinds of aggregates are in reality but different degrees of the same force. Secondly, the attraction which takes place between particles of a dissimilar nature, or the affinity of composition — It is this dissimilarity of particles which constitutes its basis, and without which it could not exist. This affinity is highly important, as without it, no composition or decomposition could have a being bodies would continue unchanged, and all the researches of Chemists would terminate precisely as they began. (All its phenomena are comprised in seven laws. 1.<sup>st</sup> Acts only between bodies of a different nature, and is strongest when the bodies are most dissimilar. An Alkali combines more forcibly with an acid than any other substance, these are the most opposite in their natures. An Alkali is any vegetable substance which effervesces when mixed with an acid. It is known by the following properties. It has an acid urinous taste, turns syrup of violets green, it forms glass when used with quartz substances, and also, it renders water miscible with oil. An acid is a combination of oxygen gas with any elementary substance. It possesses seven of

in the highest degree, turns blue vegetables into red, and forms a rapid combination with an alkali.

2<sup>d</sup> Law. It acts only between the smallest particles of bodies. Here we may observe a striking difference between the two affinities, for whenever the force of one is weakest, that of the other is always strongest. The force of aggregation exists less in gases than any other body, and these by the affinity of composition combine with other bodies with the greatest facility imaginable. Hence it is infered as an axiom, that the affinity of aggregation is inversely as that of composition, and vice versa.

3<sup>d</sup> Law. It unites more than two bodies. This law is indeed very confined. We are acquainted with many combinations of two bodies, a few of three, but scarcely any of four. Metals alone exhibit an instance of the last.

4<sup>th</sup> Law. In order that it may take place between two bodies, one at least must be in a fluid state. Corpora non agunt nisi sint fluida. There are some bodies, which, when reduc'd to a very fine powder, will form a compound. In instances of this kind, during their state of pulverization the atmosphere is attracted by the particles whose moisture in some measure combines them and renders them still subject to the last law, and in fact this law acts with very little exception. When a solid is so suspended in a fluid as to disappear it is called solution. This phenomenon is easily accounted for by the superiority of the affinity of composition over that of aggregation. Transparency is the test of solution. The action of a solid and fluid in solution is perfectly reciprocal, the part perhaps of the solid body is the greater, favors tendency to combine with the fluid is so great, as to prevail over it, and destroy its aggregation entirely. When so much of a solid is suspended in a fluid that it will dissolve no more, it is then said to be saturated, and this quantity is usually one fourth. By taking equal quantities of the combination, and finding that they are equally impregnated with the solid, we conclude that the solid is

Solution is the attenuation, the division, and entire disappearance of a solid body, when immersed in a fluid.

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5<sup>th</sup> Law. When two or more bodies are combined by their affinity, their temperature changes at the instant of their union. This phenomenon is explained by considering heat as a distinct body having a considerable part to act in all chemical operations, and from the absorption, or disengagement of this body arises a temperature. Now water in a glass tube, reaches the height to which it rises; put salt in water, and it will rise the marked height, then graze a little sink below it, and at last will rise to the original height, and be of the same temperature with the surrounding atmosphere. As water can only be dilated by heat or compressed by cold, this rising plainly indicates a change of temperature.

6<sup>th</sup> Law. Two or more bodies united by the affinity of composition form a substance whose properties are different from those which either of the others possessed before their union. It was the opinion of ~~and his followers~~, that compounds always partake of the properties of their constituent parts. But there are many phenomena that incontestably establish this law. Things that have no taste in their simple state acquire a strong one when combined. Others by combination lose their former taste. Some that are odoriferous when separate, become insipid when united with other bodies & the contrary. A few grains of mercury, or oxygenated muriatic acid taken in a little water can be no way hurtful, but combine them so as to form the oxygenated mercurial muriatic (or corrosive sublimate) and they make an infallible poison. If we attend to the phenomena exhibited by bodies in combination, we shall readily perceive that their taste, their form, and their consistence are changed by composition, and we cannot establish any rule to indicate, a priori, all the changes which may arise, and the nature and properties of the body which may be formed.

7<sup>th</sup> Law. Every individual substance has its peculiar affinity with various substances presented to it. If all bodies had the same degree of affinity with each other, no change could

take place amongst them: we could not be able to displace any principle by applying one body to another. Nature has therefore wisely varied the affinities, and appointed to each body its relative with all those that can be presented to it. It is in consequence of this difference in the affinities, that all decompositions are made in chemical operations. — The affinity of composition has received different names according to its effects. It is divided into Simple affinity, Double affinity, the affinity of an Intermedium, and Reciprocal affinity. Two principles united together, and separated by means of a third, afford an example of simple affinity: thus an acid has to a metal an affinity equal to A, an alkali equal to B to an acid; the alkali will separate the acid from the metal with a force equal to 2. Bergman has given the name of Elective Attraction to this force; a name well adapted to it, as it appears to have a choice in uniting with one substance rather than another. The body which is disengaged or displaced, is known by the name of the Precipitate; that which causes it to fall, is called the Precipitant; and the action itself called Precipitation. Dissolve silver in nitric acid, and add copper; the silver will be precipitated, and iron and the copper in turn will fall to the bottom. When the combination of two principles cannot be destroyed by means of a third or fourth body separately applied, but by taking them both united to separate the compound, or precipitate one of the bodies, it is called double affinity. Thus the sulphate of pot ash, or vitriolated tartar, is not completely decomposed by the nitric acid, or by lime, when either of them is separately applied; but if the nitric acid be combined with lime, this nitrate of lime will decompose the sulphate of pot ash. In this last case, the affinity of the sulphuric acid with the alkali, is weakened by its affinity to the lime. There are cases in which two bodies having no perceptible affinity to each other, obtain a disposition to unite by the intervention of a third: thus water is rendered miscible with oil, by uniting it with an alkali. This is called the affinity of an intermedium. Reciprocal affinity is,

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when a compound of two Acids being separated by a third, is again destroyed by the separated body, so that there seems to exist a reciprocity in its effects: thus the vitriolic acid has a stronger affinity than the nitrous Acid for fixed alkali, and it will separate this alkali when combined with the last acid. But the nitrous acid can in its turn separate the vitriolic acid, if the nitrous acid be heated— Some Chemists have supposed this from the Newtonian attraction, on account of their analogy to be the same, and that the greater the gravity of any body, the greater also was its affinity. The cause of this latter is altogether unknown, however there is a remarkable difference observable in its laws and those of attraction. The latter acts between the largest masses, affinity takes place only between the smallest particles. Attraction operates at the greatest distance, affinity only in contact. Hence we see that if affinity be not entirely distinct from attraction, it can only be a modification of it.

Alkalies are fixed or volatile: the former are not volatilized even in the focus of a burning mirror, and emit no characteristic smell. The latter are reduced into vapours, and emit a very penetrating odour. There are only two kinds of fixed alkali, vegetable and pot ash, and mineral, as Soda, volatile (and sal ammoniac—

(19)

# Lecture 4<sup>th</sup> Gravitation

Attraction of Gravitation is that force by which distant bodies tend towards one another. But do bodies really attract each other, or are they urged by an exterior force? Of this we are completely ignorant. This impulsion has only been supposed, but never proved. Newton himself has never given attraction as the physical cause of the gravity of bodies, he only uses that word to express the fact, and not to assign a reason for it. Thus he says in his principles of philosophy. "I use in the same sense, attraction, and accelerating, or moving, impulsion; and I use indifferently the words, impulse, attraction, and propensity to a centre — for I consider these forces mathematically and not physically. The reader then should guard himself against believing that I have desired to express the cause, or assign the physical reason for this kind of action; and when I say centres attract, or when I speak of their force, he must not think that I have intended to attribute any force to those centres, which I consider only as mathematical points. It follows therefore, that we do not know what is the physical cause of gravity, tho' many systems have been invented to assign a reason for it. But if any one wishes to see these hypotheses, he may consult Des Cartes, and also see what Newton has said in his mathematical principles of Natural Philosophy.

Let us then, consider gravitation agreeably to the Cartesian system, as a universal property of matter; so that by this property, not only one body tends towards another, but the parts of the same body all tend to each other.

We see that all bodies fall to the earth, when their support is removed; that thrown upwards, they invariably return. We also see, that all motion is performed in straight lines, unless there be some cause which turns the moving body from that line. Hence bodies which in their



motions describe curved lines, must be forced into that  
 direction by some adequate power which acts constantly  
 upon them. But the planets make their revolutions in  
 eccentric orbits, or nearly in circles. There is therefore some  
 power, whose continual action prevents them from flying  
 out of their orbits or the circles in which they move, and from  
 moving on forever in straight lines. It is that power, what  
 we may be the cause of it, that we call gravity. In reality,  
 the planets could not continue one moment in their orbits,  
 if there were not some force which retained them, or which  
 urged them towards the centre of their revolution. This force  
 then, of gravity, is universally acting, not only upon our earth,  
 but throughout all the planetary system; and tho' we are  
 ignorant of the cause, still we must admit its agency.  
 We shall see according to what laws this agency is exerted.

It happens frequently, that gravitation acts alone  
 upon bodies, and that they fall according to the laws which  
 we shall mention. All other times, gravitation acts upon  
 bodies conjointly with some other power; which produces a  
 compound motion. We must speak of these two cases separately.  
 Let us begin with the first, (ie) let us examine the  
 phenomena which take place, when gravitation acts alone  
 upon bodies. 1<sup>st</sup> We must not confound gravitation & weight.  
 They express two different things. The gravitation of a body  
 is the force which solicits it to descend, and its weight is  
 the sum of the gravitating particles contained in its mass.  
 Gravity belongs equally to all the particles of the same body.  
 This force neither diminishes, nor augments by their union, or  
 their separation; but the weight of a body changes with  
 the quantity of matter which composes it. We may then  
 say, that altho' a small body has less weight than a large one,  
 yet it has as much gravity, for they will both fall to the  
 earth, from any elevated place, with the same velocity.

2<sup>o</sup> It is necessary to consider in gravity, what we  
 consider in all other powers. viz. 1<sup>o</sup> Its direction. 2<sup>o</sup> Its  
 intensity, i.e. the measure or quantity of attraction upon  
 bodies.

1<sup>o</sup> Its direction is always perpendicular to the horizon. We express this direction still further, by a tendency to the centre of the earth, which would be precisely the same as this, if the earth were spherical; for then every line perpendicular to its surface would only be an extension, or prolongation of a radius. But the earth being a spheroid, flattened at the poles, lines perpendicular to the surface do not all meet at the centre, but at different points, which form a space or circle at the centre. But as this space is very small, we may without any sensible error, regard the centre of the earth as that to which heavy bodies tend.

With respect to the intensity of this power, or the measure of its action upon bodies, there are many questions which it is necessary to examine, and to resolve - 1<sup>st</sup> It is necessary to know, whether the action is the same in all bodies, or whether it tends to make all bodies descend with equal velocity. 2<sup>nd</sup> Whether the measure of this action is the same at all times. 3<sup>rd</sup> Whether it is the same in all places. 4<sup>th</sup> Whether it varies in the same body. 5<sup>th</sup> In the case where it varies, whether it augments or diminishes; and 6<sup>th</sup> In either case what is its progress.

Experiment only teaches very nearly, what space a body will fall through in a given time in consequence of its gravity; because it has always to overcome obstacles inseparable from its natural state, as, for instance, all bodies which obey any other power - such as the resistance of a medium thro' which the body moves; which resistance varies. 1<sup>st</sup> with the density. 2<sup>nd</sup> the figure of the falling body. 3<sup>rd</sup> the proportion of its mass, or quantity of matter, to its volume or bulk. 4<sup>th</sup> the proportion of its weight, which it loses in air. All these circumstances prevent us from knowing precisely the primitive measure of the action of gravity upon bodies. We know only, that in the latitude of Paris, a body which has but little bulk, and much mass (as a ball of lead) will fall through the air, at the rate of 15 Paris feet in the first second of its fall. The Paris foot is to the English, or our foot, as 233 to 278, which makes 15 Paris

feet equal to 16 English.

The measure of the action of gravity. Is it the same in all bodies? It was for a long time supposed, that gravity and weight were synonymous, and that a body had a tendency to fall so much the greater, as it has more mass or weight. This was probable. In effect, it was seen (as we still see) in air, that a body less dense, as a feather, will fall with less velocity than one more dense, as a stone, or a piece of metal. Galileo finding that the difference of their velocity was not in proportion to their masses, first imagines that the difference of their fall arose from the resistance of the air, which acted more powerfully upon bodies which had less mass, in proportion to their surface. The experiment made upon a guinea and a feather confirms the justness of this reasoning. In vacuo all bodies fall with equal velocity. The measure of the action of gravity is then the same in all bodies, and it is only the resistance of the air, which is the cause of the difference of their fall in plums, or through the atmosphere.

The measure of the action of gravity is the same at all times. There appears no variation in this respect.

Is the measure of the action of gravity the same in all places? Regarding the centre of the earth as the point to which heavy bodies tend, it was suspected that at different distances from this centre, the intensity of gravity would not be the same. But that it would act with less force, as bodies were farther removed from it. Accordingly experiments were made at the greatest heights and greatest depths which could be found, but no sensible difference could be noticed. It was then thought that gravity was uniform at all distances. But such an error could not escape the penetrating eye of Newton. He has on the contrary shown, that gravity acts so much the less upon bodies, as they are more remote from the centre of the earth, and has proved according to what law that diminution is regulated, viz. that gravity decreases as the squares of the distances increase. No gravity exists a power equal in all directions,

it must necessarily decrease according to that ratio.

Sir Isaac Newton shows that if the moon were abandoned to the force of gravity alone, it would fall to the earth, and pass over 16 feet and one inch in the first minute of its fall. But this is the space, which a body near the surface of the earth runs over in consequence of gravity, in the first second of its fall; and if it fell freely during one minute, it would run over (in consequence of the momentum in which its fall would be accelerated, as will be hereafter shown) 3600 times that space. A body which should fall from the moon towards the earth, would, therefore, fall 3600 more slowly than one near the earth. But the distance is nearly 60 times as far from the centre of the earth, as that of bodies upon its surface. And 3600 is the square of 60—of course, gravity decreases as the squares of the distances increase. But how is this law collected? 1<sup>st</sup> from geometrical reasoning upon straight lined emanations of any force, and 2<sup>nd</sup> from observations upon the revolution of the moon.

We have not elevation sufficiently high to establish by experiment this theory of the direct fall of bodies; but Messrs Bouguer and Condamin have supplied the want, by the following ingenious experiment. They caused a pendulum to vibrate during the revolution of a fixed star (we may here observe that every vibration is the effect of gravity) first at the foot of one of the Cordilleries, then at the top, and measured the difference of the perpendicular altitude of these two stations. The number of vibrations was less during the same time, at the top, than at the base of the mountain, and the difference accorded with the theory of Newton. A body which weighs 20 lbs. carried to the top of a mountain three miles high, would weigh 16 lbs. only. The intensity of gravity ought also to be different, in different climates of the earth. 1<sup>st</sup> on account of the greater velocity of the earth near the equator which communicates a centrifugal force directly opposite to gravity under the equator, and obliquely to it every where else, and so much the more obliquely as we approach the poles. This may be illustrated by a common globe. Bodies then fall more slowly near the equator, than towards the poles, and this in effect has been proved by experiments made in Cayenne.

in 1672 by Richi. He observed that a pendulum which vibrates at Paris, measured a longer time, or vibrates more slowly at Cayenne: a proof that the gravity was less. This experiment has been repeated by many good observers, but particularly by the academicians who went to Paris, and those who went to a very high north latitude, to ascertain the figure of the earth. And it has always been proved, that bodies fall more slowly near the equator than near the poles, and that this retardation diminishes, as the latitude augments. It is, indeed, this experiment which has proved demonstratively the revolution of the earth upon its axis, and that it is not truly spherical.

Does the measure of the action of gravity vary in the same body? In this we may answer, that it will vary as the body is set in motion, as the proportion of its mass to its volume varies, and also as its figure varies. But these are only accidental variations, which would have no effect in an unresisting medium.

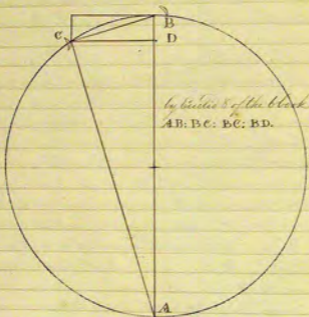
There is, however, a variation which depends solely upon gravity; for a body in falling will have its velocity continually increased. Every one knows, that the higher the place from which a body falls, the greater is its shock. And the intensity of this shock, or blow, can result only from an increase of velocity.

The intensity of gravity is then always increasing in the same body which it falls. But according to what law does its velocity increase? Experiment shows that the increase of velocity is proportioned to the altitude of the fall, and not to its duration. If we let fall different bodies of the same figure from altitudes which are in the increased ratio of their masses, they will all produce the same effect. They, they have also an equal quantity of motion, which would not be the case, if the velocities acquired at the end of each fall, were not in proportion to the altitude of their falls. A large mass, therefore, coming from a less height, will produce the same effect as a small mass coming from a greater height. We may, of course, choose between these two means, either to augment the mass, or to augment the velocity. But it is often advantageous to substitute weight for elevation.



BC or those areas are as the squares of the distances from A. This is easily shown thus; AHB, ACD being equiangular triangles (Eucl. P. 29 B. 1) we have (Eucl. P. 4 B. 6) AB: AC :: BH: DC. But BH, DC, are the homologous sides of the similar plane figures BC and KD; and (Eucl. P. 26 B. 6) those figures are as the squares, or in the duplicate ratio of those sides — This diminution of intervisibility, in proportion of the squares of the distances from the centre of emanation, seems to take place not only with the force of gravity, but also with all sorts of emanations from a centre, such as light, sound &c.

Calculation for determining the distance that the moon would fall towards the earth in one minute of time, if acted upon by gravity alone.



AB is 480000 miles equal the diam<sup>r</sup> of the moons orbit with respect to the Earth and supposing her periodical time 27 days 7 hours. Required her motion in one minute of time in her orbit, and the versed sine of that arch: Viz the space she would fall thro' by the force of Gravity alone!

$7 \times 240000 \times 57 = 9511200$  the orbit in miles. Then  $9511200$  divided by the minutes in  $27 \frac{7}{24}$  viz by  $39360$  gives  $38.81$  miles.

Then 33.16 miles squared gives 1100.64 and this multipl<sup>d</sup>  
by 5280 feet in a mile gives 7810026.688 feet which divided  
by 500000 mile gives 16 feet  $\frac{8}{10}$ .

AB The result is too great by reason of the ratio 1:377 having  
been used instead of 1:3.1516.

The moons period from change to change is  $29^{\text{d}} 12^{\text{h}}$  - suppose  
the suns app<sup>t</sup> motion one degree per day

then as  $360^{\circ} + 29^{\circ} : 29^{\text{d}} : 12^{\text{h}} :: 29^{\circ} : 53 \text{ hours} - 2^{\text{d}} : 5^{\text{h}}$   
then from  $29^{\text{d}} 12^{\text{h}}$  hours sub  $2^{\text{d}} : 5^{\text{h}}$  there remains  $27^{\text{d}} 7 \text{ hours}$  for  
the moons periodical time.

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# Lecture V.

## Magnetism.

The name magnet is said to have been taken from the name of a shepherd by whom it is supposed to have been discovered in some Ides. Some suppose it to have been first found near Thracia a city of Magnesia, and hence it has been called *Lapis Thracicus*. Whatever the magnet be called, it is found to be a mineral substance (see hairs as almost to resist the fire) of a dark grey, and sometimes nearly black, colour. It is an iron ore which attracts iron and ferruginous bodies, and them only, if we except two substances (*viz.* Nickel and Platina) which it has been found to attract in a small degree.

It is very probable that this substance received the name of magnet, on account of its peculiar and astonishing properties. So that we should search no higher for its etymology, than the Latin word *magnus*, great.

There are two kinds of magnets, natural and artificial. The natural magnet is the load stone dug out of the earth. The artificial one, is an iron bar, to which magnetism has been communicated. And here it may be observed that the artificial is by far more powerful than the natural magnet.

The common properties of a magnet are six in number, *viz.* Attraction and Repulsion, Direction, Inclination, Declination, and Communication. And there is no instance of a magnet possessing one without all these properties. There are many laws by which the magnetic properties are governed.

1<sup>st</sup> The tendency of the magnet to such bodies as it is said to attract, is mutual and equal between it and those substances. This may be seen by a variety of experiments: thus, two curing needles (one of which shall be touched with a magnet) stuck through small pieces of cork, and put near each other in water, will be observed mutually to approach until they come in contact &c.

2<sup>d</sup> If a magnet be suffered to traverse freely, it will arrange itself so that one will constantly point North, and the other South. This is called magnetic polarity. The end that points north, is called the north pole,

and the other on that point south, the south pole, and the middle is called the equator. This is the most distinguished and the most useful property of the magnet. By the aid of the magnetic compass (which is an artificial steel magnet so placed in a box, as to remain horizontal in any position of the ship) discovery has been discovered, and is enabled to exchange commodities with the most distant nations.

It is to be observed that the poles of the magnet are endued with the strongest attraction; for a key, or any bit of iron suspended at one of the poles will drop when moved towards the equator. To find the poles of a natural or artificial magnet, let it be placed upon a plane and sprinkled with steel filings, these filings will so arrange themselves as to discover the poles. Still we may not know the direction from the south pole. This may be found by placing the magnet on a thin leaf of gold lying on water. It frequently happens that the same magnet has several poles, which principally arises from its irregular shape. The phenomenon of the magnetic polarity is accounted for from the hypotheses that the earth itself is an immense magnet, with a south polarity at its north pole, and a north polarity at its south pole.

3<sup>d</sup> Similar poles repel, and dissimilar attract. If the north end of a magnet which traverses freely, bring the north end of another magnet, and the former will be repel<sup>d</sup>, but if the north end be applied to the south end the latter will be attracted. If the north or south end of a magnet be brought very near the similar end of a needle it will be attracted; which is an apparent exception to the general law. It is however only apparent; for in truth when the larger magnet is in contact with, or very near, the smaller, it communicates to it a contrary polarity. This is evident by experiment.

4<sup>th</sup> The interposition of other bodies does not interrupt the magnetic attraction. A needle in a plate will be attracted by applying the magnet under it; and even if the plate should rest on a table, the needle therein will be strongly attracted by a magnet under the table.

5<sup>th</sup> Each pole attracts and repels at equal distances in all directions.

6<sup>th</sup> Attraction of magnetism decreases as the squares of the distances increase, and vice versa, according to some philosophers. D. All says that different magnets have different attractive forces; and that the attractive force of the same magnet is different at different times. Balance a bar of iron in a pair of scales, place a magnet at the distance of one inch from

the bar and as much weight in the opposite scale as will balance the magnet free then, according to the law, if the magnet be removed to the distance of two inches, a fourth part of that weight ought to preserve the equilibrium. The experiments, according to Dr. H., sometimes will, and sometimes will not answer, the conclusion that this law is true, has been drawn from observing the number of vibrations that were made in the same time by a needle placed at distances which were as 1 to 2.

7<sup>th</sup> The magnet will communicate its properties to iron without any diminution of its own. Upon this property depends our power of making artificial magnets.

8<sup>th</sup> Iron acquires and loses magnetism sooner than steel, soft iron sooner than hard, and these tendings to lose is directly as their parts, to acquire. It is remarkable also, that small magnets have greater strength in proportion to their size than large ones. A magnet in 18<sup>th</sup> Bezel's ring could support 28<sup>th</sup> times its own weight. It weighs 5 grs. and could raise 74.

9<sup>th</sup> It attracts iron in a duplicate ratio of its communicative power.

10<sup>th</sup> A magnet will communicate its properties to iron without touching it. In communicating magnetism to iron, the N. end of the magnet will give a S. polarity, and vice versa. Let a magnet be placed upon a table so as to traverse freely. Place the end of a bar of iron near either end and say N. (Bring) near the opposite end of the iron bar, another magnet's S. end, in which case the end of the iron bar next to the communicating magnet, will acquire a south polarity, and the other end of course, a north. Now the last end was opposed to the N. end of the traversing magnet, which will be repelled, and the repulsion could not take place, if the iron bar were not magnetic. There is another (and a more satisfactory experiment) which proves this law. Place a magnet at a small distance from a bar of soft iron (suspended for convenience), and it will communicate attraction sufficient to support a small scale or bit of iron, at the end of the bar.

Some authors suppose that there is a current of magnetic fluid circulating constantly from one pole to the other. By the following experiment, however, this supposition is manifestly proved to be incorrect. If a magnet be put into water, so as barely to be covered, and steel filings dropped on the surface, these filings will be seen to separate at the equator, and approach each pole, where every particle becomes a

distinct magnet, and presents a contrary pole to that by which it is attracted, to the magnet under water. The strength of magnetic attraction being accumulated at the poles or ends, these particles can never circulate around the large magnet, but will ever remain fixed to it at those poles on account of the superior attraction.

The earliest knowledge which man had of the use of the magnet (or of its directive property, for its attractive power was known to Thales, and others of the ancients) cannot be traced further back than the 13<sup>th</sup> century. It was not till after this time that it was employed in commerce, to the advancement of which it has greatly contributed.

Some attribute the invention of the compass to Beshar de Giza who in Barroli's opinion has the best title to it. D. Gilbert says that Saul Terentius brought it from China into Italy in the year 1266. This testimony appears that in the east Indies about the year 1200, he saw a magnet contrived like those now used, employed by a pilot. Mr. B. Quaker relates that in the year 1567 he saw two east Indians who mentioned to him a contrivance, different from the compass, for using the magnet in navigation. These observations are in date posterior to the use of the magnet in Europe, and therefore, conclude nothing as to the invention. The Spanish Jesuit, Benedit, and Elachi affirm that they know the use of the compass, and that his subjects actually used it in navigation. However, the original invention is attributed, with great probability, to the Chinese. The needle does not always point directly N. and S. but sometimes declines to the E. or W. This is called the variation or declination of the needle - It is the angle made by the magnetic and the true meridian. We always reckon the variation at the N. point. The variation is different at different times and places, so that there is a variation of the variation. In 1692 in Williamsburg when the college lands were surveyed the variation of the needle was 5° west. At present (1807) it is

The needle therefore in about 112 years has travelled nearly  
In Europe the variation is to the west, in America to the E. the variation at London and Paris is different. There are four places where the needle is stationary, & its variation entirely ceases. 1<sup>st</sup> At a particular point in the Atlantic ocean. 2<sup>nd</sup> Along the American coast. 3<sup>rd</sup> In the Indian ocean, near the Philippine isles, and 4<sup>th</sup> In the sea. For this phenomenon the diligence of philosophy has never been able to

accounts Columbus first discovered the variation in 1492. and soon  
 Sebastian Cabot made some particular observations on it in the  
 year 1500.

To find the variation of the needle many methods are mentioned  
 I will select one of the most simple On the 26<sup>th</sup> of March and 2<sup>d</sup> of Sept.  
 the sun rises precisely in the east. Place the E. and W. points of a  
 compass directly in a line with the rising sun; the N. and S. points  
 will then be on the same meridians, and the variation of the needle  
 will then be seen in the graduated circle in which it plays. But  
 the needle has also a diurnal variation. From 8 till 3 o'clock  
 the needle travels a little way W. and from 3 till 8 o'clock it  
 travels E. It is remarkable that the diurnal variation is extremely  
 affected by the Aurora Borealis. It is observed to be the greatest in  
 the months of June and July, and least in the months of January  
 and February. In the former months, it is about 15°, in the latter  
 6 or 7°.

A needle if suffered to play freely will dip. This is called the  
 inclination of the needle. The dip is greater or less as it approaches  
 the poles or the equator. On the N. side of the equator the N. end  
 dips, and on the S. side the S. At the equator the needle is horizon-  
 tal. At Williamsburg it dips 87°, and at London 72°. At the poles,  
 the needle would stand perpendicular. Three sewing needles rendered  
 magnetic, and suspended by threads, one over each pole, and one over the  
 equator of a large magnet, will exhibit a clear proof of this pheno-  
 menon. Those over the poles will be perpendicular, while that  
 over the equator will remain perfectly horizontal. The dipping nee-  
 dle is proposed to be used for determining the latitude of places. But  
 what will not fail to obstruct this use, is, that it is not uniform  
 in receding from, or approaching towards, the equator of the earth,  
 nor even in the same place at different times. In London about  
 the year 1576 the N. end of the dipping needle stood 11° S. below  
 the horizon and in the year 1775. 72. S. E.

It has been observed that the artificial magnets are stronger & more  
 useful than the natural ones. Hence it is necessary that we should be  
 acquainted with the method of making them, which are several. It  
 with the use of the natural magnets. It appears that the best manner  
 of making artificial magnets, consists in applying one or more

powerful magnets to pieces of the hardest steel, because these pieces will thereby acquire a considerable magnetic power, and retain it for a very long time. In this operation care must be taken to apply the N. pole of the magnet to the extremity of the steel which is required to be made a S. pole, and to apply the S. pole of the magnet to the opposite extremity of the piece of steel. 2<sup>nd</sup> Without the aid of a natural magnet, or the method of magnetizing steel without any magnet. Strictly speaking, this method does not exist; for there is no magnetism communicated, but by the action of a magnet, and in the above mentioned method the magnetic power is originally communicated by the earth, which is a real magnet, of which (as has been already said) a S. magnetism is attributed to its N. pole, and vice versa. By this it is meant, that the earth has a magnetic polarity, and that its poles are directly contrary to those of the needle; and as we call one end of the needle a north magnetic pole, we must of necessity attribute a contrary polarity, viz. a S. magnetic polarity to the astronomical pole, or northern part of the earth. It follows that the astronomical S. pole, or southern part of the earth, must be possessed of a N. magnetic polarity. That the earth is really a vast magnet, is evidently and easily shown by the following experiment. A straight bar of soft iron being kept in a vertical position, viz. with one end towards the ground and the other upwards, you will find that the bar in that situation is magnetic, the lower extremity (in the northern part of the world) being a N. pole capable of attracting the S. pole of a magnetic needle, and of repelling its N. pole, and the upper extremity becoming a S. pole. If you invert the bar its polarity will be instantly reversed. The explanation of this curious phenomenon is easily deduced from the preceding laws, for since the northern part of the earth is possessed of a S. polarity, the lowest part of the iron bar, by long contact with it, must acquire the contrary, viz. a N. polarity, the other extremity of the bar being of course a S. pole. It follows likewise (and is confirmed by actual experiment) 1<sup>st</sup> That in the southern parts of the earth the lowest part of the iron bar acquires a S. polarity. 2<sup>nd</sup> That on the equator the iron bar must be kept horizontal, to acquire magnetism from the earth; and 3<sup>rd</sup> That the most advantageous situation is not the perpendicular, but a little inclined to the horizon. In short, in every part of the world, the bar must be placed in the magnetic line, to wit, in the direction



parts of the earth, and which are frequently magnetic, prove beyond a doubt, that the earth is a magnet, but irregular magnet, and that its magnetism arises from the magnetism of all the ferruginous bodies that are contained in it; so that the magnetic poles of the earth must be considered as the centres or collected points of all these magnetic ferruginous substances. It follows likewise, that according as these masses of iron are affected by heat or cold, by decomposition, by mixture with other substances, by alterations, by earth quakes or mechanical derangement &c. so the magnetic poles of the earth must change their situation: and this is the cause of the variation of the magnetic needle. The properties of a magnet are not affected either by the presence, or the absence of air. — The magnet is found in great quantities, in the countries of Silesia, Austria, and Prussia, in the state of Virginia.

The great desideratum in magnetism is, to know the cause of the magnetic attraction, repulsion &c. The human ingenuity has contrived a number of hypotheses in explanation of these phenomena. Healey supposes, that there was a large magnet inclosed in the earth, which not being fixed to its external surface, was movable within it, and produces all the magnetic phenomena. Some philosophers (among whom was Bitterbergh) imagined that the pores of all ferruginous bodies were full of a viscid fluid which permitted the fluid to pass through them one way, but by obliquity immediately prevented it from returning. Boscovich supposed from the experiment of placing a magnet on a sheet of paper, and sprinkling iron filings over it, which would arrange themselves almost circularly round it, that there was a current of magnetic fluid issuing from one pole and entering the other. but if this were the case, the iron filings would be all driven upon one of the poles. The theory of Laplace is founded upon the strong analogy between magnetism and electricity. He was led to imagine that there exists a fluid productive of all the magnetic phenomena. That like the electric fluid, it is as elastic as to penetrate the pores of all bodies, is elastic, and highly repulsive of itself. He also supposes that there is a mutual attraction between this fluid and iron, or ferruginous substances, but that no other bodies have an action upon it. Thus when a ferruginous body is not magnetic, this fluid is equally diffused throughout its parts, in which state they show no attraction or repulsion: but when this fluid is driven to one end, the body becomes magnetic, one extremity being overcharged, and the other undercharged.



There is no attraction between the overcharged extremities of two magnetic bodies, on account of the attraction between the fluids and the matter of the body. But the cause differently occurs as in electricity to account for the repulsion between the undercharged extremities. A piece of iron is rendered magnetic by the action of a magnet, because when the overcharged pole is presented to it, the surplus of magnetic fluids in that pole, repels the fluids from the nearest extremity of the iron, which therefore becomes undercharged to a more remote part of the iron. If the undercharged pole of the magnet be applied, then its matter attracts the magnetic fluids of the iron to that extremity of the iron which lies nearest to itself.

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# Lecture VI.

## Of Motion.

Motion is considered as absolute, relative, or apparent. All motion is in itself absolute, or the change of absolute space. But when the motion of bodies is compared with that of each other, then it is relative, or apparent only. It is relative as it is compared with another, and apparent only in as much as not its true or absolute, but the sum or difference of the motion is perceivable by us.

Nearly all the phenomena of nature are owing to motion. The appearance and disappearance of the heavenly bodies, the increase of animals and vegetables, the composition of complex substances, all arise from motion, the laws of which may therefore be looked upon as the foundation of natural philosophy.

Motion is either simple or compound. It is simple, when there is one uniform impulse, and compound when several powers act together in many different directions. In treating of motion we are to consider seven things, 1<sup>st</sup> The power, or force that causes a body to move. 2<sup>nd</sup> The mass, or quantity of matter. 3<sup>rd</sup> Its direction. 4<sup>th</sup> The space it moves over. 5<sup>th</sup> The time it takes to move. 6<sup>th</sup> Its velocity, and 7<sup>th</sup> Its momentum. The moving force or power which causes motion does not communicate any thing to the body (unless giving it motion can be said to be communicating) it only moves it through a certain space in a certain time, after which a body being left to itself will continue to move at the same rate in an unresisting medium, that is, it will continue to run over like spaces in like portions of time, and that merely in consequence of its vis inertia, of which vis inertia we do not pretend to know any thing more, than that it is a general property of matter.

The quantity of matter in bodies is estimated by their weight, and is often termed the mass. Bodies resist equally whether at rest or in motion, and the force of resistance is always in proportion to the quantity of matter; the greater the mass, the less motion they receive from force. The velocity is always inversely as the quantity of matter; for if two bodies one of which weighs 8 lbs and the other 2 lbs be moved

with a perpendicular  $AD$ , the latter will pass over double the space of the former in the same time.

The direction of motion is the position of the line along which it is performed. When the motion is curvilinear, the direction at any instant of time is the position of a tangent to that point of the curve where the moving point is situated.

The space thro' which a body moves is the line it runs over. The time a body employ in moving over space, is greater or less in proportion to the length of the space, and the velocity with which it moves.

The velocity of bodies, is their power of passing over space in a given time; so that it always has relation to space and time. If two bodies run over equal spaces in equal times, their velocities are equal. If over unequal spaces in equal times, or equal spaces in unequal times, then their velocities are unequal. When the velocity of a body is continually increasing, it is said to be accelerated, and the farther it moves, the greater is its velocity.

The momentum of bodies, is the force arising from the sum of their moving particles, and is found by multiplying the velocity into the quantity of matter. Thus a body weighing 2 lbs, moving with a velocity equal to 6 degrees, will have a momentum equal to 12. By increasing the velocity of a small body, it may be made to possess as much momentum as a large one. A common ball moving 1112 in a second, and weighing 2 lbs, will have a momentum equal to that of a battering ram weighing 1112 lbs and moving at the rate of 1 foot per second.

In computations relating to force, motions, times &c. the proportion of the quantities to each other is considered, and not the quantities themselves. In such computations, therefore, when any two quantities are compared together, we may substitute any other two quantities which have the same proportion to each other, as numbers, lines &c. It follows from what has been said on the quantity of motion, that if the velocity of a body increases, while its mass remains the same, its force will be augmented, as the velocity is increased. As if several bodies of the same mass move with different degrees of velocity, their force will be as the velocities with which they move. If several bodies are possessed of the same velocity, their force will

to as their masses, if they will have as much more force as they have more mass, being composed of a greater number of parts animated with the same force. Simple motion (it has been said) is that which is produced by one force acting, instantaneously on the body, and causing it to describe a right line with an uniform velocity, i.e. describing equal spaces in equal times. It will be shewn, that there is no single motion, but what may be considered as resulting from various forces tending jointly to carry the moving body to the same point; and reciprocally, that there is no rectilinear uniform motion so compounded, but what it may be considered as produced by the simple action of one force.

## Laws of Motion!

1<sup>st</sup> Every body will continue in its present state, whether of rest or motion, unless it be compelled to change that by forces imposed. 2<sup>d</sup> Every motion, or change of motion in any body must be proportional to, and in the direction of, the force imposed. This is the immediate consequence of the axiom that, "the effect is always proportional to the cause." For instance, if a certain force produces a certain motion, a double force will produce double the motion, a triple force triple the motion &c. 3<sup>d</sup> Law Action and reaction are equal and contrary to each other. Action and reaction are correlative. One cannot exist without the other. Assistance or reaction, is a necessary condition to action: action, indeed, becomes reaction by a new change of circumstances. There are various phenomena which establish the universality of this law. When a cannon is discharged, the rarified powder acts equally on the ball and the breach of the gun. The reaction of water on the oar occasions a boat to advance, & communicates to it as much motion as it receives. The fish performs with its fins, & the aquatic birds with their feet, what the waterman effects with his oar, the mutual action and reaction impelling them along. Birds support themselves, and pass thro' long tracks of air, notwithstanding the weight of their bodies much exceeds that of an equal volume of the fluid in which they move. If their wings strike, and push the air towards the earth, its reaction supports their bodies, and carries them to a height.

General law of compound motion. — Every body

solicited to move by the simultaneous action of different forces acting in different directions, will take a mean direction between what each power tends to communicate to it, and will move with a velocity proportional to the force acting, respectively; for as the body cannot move in more directions than one at the same time, it must move in the direction resulting from the combination of the acting powers. Thus if two forces act at the same time on any body, and in the same direction, the body will move with a velocity equal to the sum of the velocity of the two forces acting upon it. If the forces are unequal, and acting in opposite directions, the body will move in a direction of the strongest, with a velocity equal to the difference of the velocities arising from the two given forces acting separately; so that the motion will take a new direction, more or less different from the former, according to the number and direction of the impressed forces. If the proportion or direction of two forces acting upon a body at the same time, be represented by the sides of a parallelogram, the diagonal will show the proportion and direction of their united forces. Let the body at *A* be impelled by a force acting upon it in the direction *AC* which would cause it to move from *A* to *C* in the same time that another force, which acts in the direction *AB*, would cause it to move from *A* to *B*. Complete the parallelogram, and draw the diagonal *AD*. This line will represent the direction



and distance the body will move in the same time, when acted upon by both conjointly.

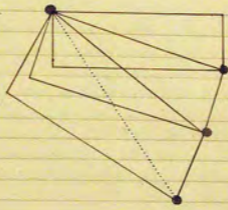
The dotted diagonal *AF* represents the direction and proportion of a body impelled by three forces at the same time in the directions



*AB, AC, & AE.*

In general, any body moving with a force represented by the diagonal of a parallelogram, may be considered as having its motion compounded of the forces represented by the sides; for the motion will be the same as if it had been impelled by two forces

proportionable to their sides— And as upon the diagonal an infinite number of parallelograms may be constructed, any single force may be considered as compounded of more forces, and thus resolved into numberless pairs of forces, acting in the direction of the sides of those parallelograms, and proportional thereto. The velocity along the diagonal is to the velocity along either of the sides, as the radius to the sine. The practice of reducing compound forces to simple, and that of finding two or more forces equivalent to one, is called the composition or resolution of forces.



Motion is simple and compound, absolute and relative, rectilinear and curvilinear. All bodies have a tendency to move in straight lines. Thus a stone in a sling, flies off in a tangent to the circle in which it moves, and its stretching the string seems to be a proof that it has a tendency to move in a straight line: but here this endeavor is only in obedience to the impulse last communicated to it, all motion being naturally rectilinear where only one power acts. Reaction and action are equal and contrary. This law is founded on reason and experience. A bullet from a gun strikes a board with a force equal to 10. The bullet will still move, but only with half its former force, viz. 10 - it is as 5; 5 is as 4; 4 is as 3; 3 is as 2; 2 is as 1. The above is an explication of the manner in which the time, space, velocity, quantity of matter, and momentum are found.

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Of the centre of gravity, and of perpendicular bodies.

The centre of magnitude of a body is that point, on each side of which are equal quantities of matter, and in bodies that are uniform and homogeneous, it is the same with the centre of motion; which is that part of any body, around which all the other parts move, but is itself at rest. And this again is the same in uniform bodies of the same matter throughout, as the centre of gravity, which is that point about which all the parts of a body do, in any situation, exactly, balance each other. An imaginary line drawn from this point to the centre of the earth, is called the line of direction. It is of great importance to understand well the nature and properties of the centre of gravity, as it is the sole principle of all mechanical motions.

The particular properties are as follows— $1^{\text{st}}$  If a body be suspended by this point as the centre of motion, it will remain at rest in any position indifferently— $2^{\text{nd}}$  If a body be suspended by any other point, it can rest only in two positions, viz. when the centre of gravity is directly above, or below, the point of suspension.  $3^{\text{rd}}$  When the centre of gravity is supported, the whole body is kept from falling.  $4^{\text{th}}$  When the centre of gravity is at liberty to descend, the whole body must also descend or fall, by tumbling, sliding, or rolling down.  $5^{\text{th}}$  The centre of gravity in regular, uniform, & homogeneous bodies, as squares, circles, spheres &c. is the middle point in a line connecting any two opposite points or angles.  $6^{\text{th}}$  In a triangle it is the intersection of two lines, drawn from any two of its angles, and bisecting the opposite sides. The centre of gravity of a polygon is found by dividing it into triangles, of which the centres may be found as above.

If the line of direction fall within the base, the body is supported; therefore, the nearer it is to the middle of the base, the more firmly the body stands. The reason of this is obvious, for as long as the line of direction is within the base, the centre of gravity is supported, since that line is conceived to pass directly from the centre of gravity to the centre of the earth, and as long as the centre of gravity is supported, so long is the body kept from falling, as has been before said. When a body slides down an inclined plane, the centre of gravity is within the base, but the inclination of the plane

being sufficient to overcome the friction of the body upon it, the weight of the body carries it down - Should the line of direction fall without the base, the body tumbles. Round bodies rest upon a very small point, and the line of direction is continually falling without the base at the slightest impulse - Hence all globular bodies are easily moved.

The centre of gravity of two unequal bodies, is much nearer to the larger than to the smaller, as the quantity of matter of the former exceeds that of the latter - An easier to find it we say, as the sum of the quantities of matter in each body, is to the quantity of matter in the smaller, so is the distance between them to a fourth proportional, which will be the distance of the centre of gravity from the larger body - The centre of gravity between three bodies is found by first getting the centre between two of them; then, - as the quantity of matter contained in the two first, is to the quantity contained in the last, so is the distance of the three from the centre of the two first, to a fourth proportional. The common centre of gravity of any number of bodies being supposed, none of these bodies can fall, which is the reason of many very surprising phenomena in nature, as the common experiment of suspending a bucket of water at the end of a stick off the table without falling.

(Communicated motion)  
1. In bodies non elastic

Those bodies whose parts yield to the impression of another body, and when compelled to change their shape do not return to it, are called non elastic. When such bodies strike, they do not rebound, but accompany one another after impact as if they were joined. This proceeds from their retaining the impression made upon their surface after the impressing force ceases to act. If all rebounding is contained by a certain spring in the surface of bodies, whereby those parts which receive the impression made by the stroke, immediately spring back & throw off the impinging body - A few this property being wanting in bodies void of elasticity, there follows no separation after impact.

When a non elastic body impinges on another which is at rest, or moving the same way with less velocity, the momentum of both bodies taken together, remains the same after impact as before; for by the third law of motion the reaction of one



being equal to the action of the other, what one gains the other must lose.

When two bodies impinge on each other by moving contrary ways, the quantity of motion they retain after impact, is equal to the difference of the motion they had before; for by the third law of motion, that which has the least motion, will destroy an equal quantity in the other; after which they will move together with the remainder, that is, the difference.

### 2.<sup>nd</sup> In elastic bodies

Bodies perfectly elastic, are such as rebound after impact with a force equal to that with which they impinge upon one another; those parts of their surfaces that receive the impingement, immediately springing back, and throwing off the impinging body with a force equal to that of impact.

If one elastic body impinge on another at rest, which is equally elastic, the first will communicate to the second all its motion - If two equally elastic bodies impinge on one another, they will (if moving with equal velocities) exchange their motion, and rebound to their former places. The action of elastic bodies on each other, is twin as great as if these bodies were void of elasticity. Thus if two iron elastic balls descending, the one through an arch of 26, the other of 15, impinge upon one another, the latter will destroy 15 of the motion of the former, and they will then move in the same direction with half the velocity that the former would move with, subtracting 15 from its motion, that is, they will move with a velocity of 11. Two elastic balls descending through similar arches with the above, would after impact move with a double velocity, or 15 in the same direction.

It has been seen that if one body fall on another of the same size, it will communicate to it all its motion, i.e. it will cause it to move through a space equal to that through which the striking body moved before impact. But it is also found by experiment that a small body falling on a large one, gives it more motion than it has itself. Thus one body impinging on another at rest of twice its quantity of matter, will cause it to move thro' more than half the space, that a body of equal quantity of matter

with the one at *rest*, would the reason of this has not been given  
 by philosophers. It is supposed to arise from a greater momentum  
 of the small body in proportion to its size, its velocity being  
 greater, as there is less surface to be resisted by the air through  
 which it moves.

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# Lecture VII.

## Central Forces.

### Of the doctrine of circular motion.

All motion is naturally rectilinear, for a bullet projected from the hand, or shot from a gun, would continue to move in the same direction it received at first, if no other power directed its course. Therefore every body which moves in a curve of any kind, does so in consequence of two powers, one putting it in motion, and the other drawing it off from the rectilinear course it otherwise would have moved in. So that all bodies which move in curve lines, have a continual tendency to go in a rectilinear course, but being acted on by a second force which gives them another direction, they are perfectly forming a quantity of every obtuse angles, or rather, a regularly curved line.

If two forces act in different directions on a body in such a manner as to move it uniformly, the diagonal described will be a straight line; but if one of the forces act in such a manner as to make the body move faster and faster, then the line described will be a curve. The tendency which a body has to fly off the orbit in which it moves, is called the centrifugal force, that which it has to approach the centre, is called the centripetal, and both together have been called the central forces. From the uniform projectile motion of bodies in straight lines, and the universal power of gravity, or attraction, arises the curvilinear motion of all the heavenly bodies. If the central forces be in equilibrium, the body will always move in a circle. It is therefore by a due adjustment of the centripetal and centrifugal forces, that harmony is preserved in our planetary system. To make the projectile force a just balance to the gravitating power, we take a planet moving in a circle, it must give such a velocity, as the planet would acquire by gravity, in falling thro' half the radius of that circle. To know the amount of a centrifugal force, three things are necessary, 1<sup>st</sup> The mass of the moving body. 2<sup>d</sup> The distance at which it revolves. 3<sup>d</sup> The velocity, and in calculating the last we must consider, 1<sup>st</sup> The time, and 2<sup>d</sup> The greatness of the circle. The following propositions are demonstrated by experiments upon the whirling table, for a description

of which are *tergiverses*. By *pericardical time* is meant, the time in which bodies perform a particular revolution. *Direct proportion* is when more requires more and less requires less; as the first term is to the second, so is the third to the fourth thus 6: 16:: 3: 2. *Inverse proportion* is when more requires less, and less more, thus 4: 6:: 2: 3.

1<sup>st</sup> Matter has a propensity to remain in its present state, whether of motion or rest. Shew'd by a body placed on the whirling table board, which being turned, has not immediately communicated motion to the body; but after the body has acquired the motion, if the board be suddenly stopped by the hand, the body will still continue to move, until stopped by friction or the resistance of the air.

2<sup>d</sup> Bodies moving in circles have a tendency to fly out of those orbits. A body placed on the whirling table, and not confined, will fly off on turning the board. 3<sup>d</sup> Bodies of equal quantities of matter, revolving in equal circles, with equal velocities, have their centrifugal forces equal. Thus two balls of equal weights, being placed at equal distances from their respective centres of motion, upon beams which have equal velocities, will raise equal weights in the towers at the same instant, upon turning the whirling board.

4<sup>th</sup> Bodies move faster in small orbits than in large ones. By shortening the axis with which a revolving body is confined to the middle of the whirling board, it will be found to move faster and faster as the radius diminishes. Those planets that are near the sun, move faster than those more remote, and not only so round the sun, because they describe smaller circles, but even move faster in every part of their respective orbits.

5<sup>th</sup> The centrifugal force of revolving bodies are in exact proportion to their quantities of matter multiplied into their distances from the centres of their respective circles. Put a ball of 6 lb. into one beam at 2 inches distance from the centre, and put a ball of 1 lb. into the opposite beam, at 12 inches distance from the centre; then the ball which is six times as heavy as the other, being at the sixth part of the distance from its centre of motion, will make in a circle of only a sixth part of the circumference of the small one. Upon turning the machine, equal weights will be raised in the towers. Thus the ball of 6 lb. being 2 inches from its centre of motion, when multiplied by its distance, gives a product of 12. And if the ball of 1 lb. be multiplied into its distance, it will also give 12. And as they revolve in equal times, their velocities are as the distances from the centre, nearly as 1 to 6.



piece of cork floating on the top — Also another tube containing the same quantity of water, with some mercury at the bottom of it. On giving the machine a whirling motion, the centrifugal force, will cause, in the former tube, the heavier body, viz. the cork, to displace the water, and occupy the upper part while the cork descends to the bottom. But in the other tube, the mercury being the heavier body, will displace the water and ascend to the top.

§ 2. If one body move round another, both of them must move round their common centre of gravity. — If a body be placed on the whirling board, so that the centre of gravity of the body be directly over the centre of the board, and the board be put in over so rapid a motion, the body will turn round with it, but will not move from its place; so as all the parts of the body are in equilibrium round its centre of gravity, and the centre of gravity is at rest in the centre of motion, the centrifugal force of all parts of the body will be equal at equal distances from its centre of motion, and therefore the body will remain in its place — But if the centre of gravity be placed ever so little out of the centre of motion, the body will fly off to that side in which the centre of gravity lies — If a small ball of one 100<sup>th</sup> part the weight of the body, at the centre of the whirling board, be attached to it, by a wire, and the table put in motion, the large weight would be drawn from its place, and together with the small ball, would be thrown off the board. This shows that the sun and all the planets move round a common centre of gravity.

The reason why the tides rise at the same absolute time on opposite sides of the earth, and consequently in opposite directions, is made plain by an experiment on the whirling table; As the moon goes round her orbit every month at the distance of 238,000 miles from the earth's centre, and of 238,000 miles from the centre of gravity of the earth and moon, so does the earth go round the same centre of gravity every month at the distance of 6000 from it i.e. from it to the centre of the earth. The earth is (in round numbers) 8000 miles in diameter its side next to the moon, is only 2000 miles from the common centre of gravity of the earth and moon, its centre 6000 miles distant therefrom, and its furthest side 10,000. The centrifugal forces of these parts are as 2000, 6000, & 10,000. That is, the centrifugal force of any side of the earth when turned from the moon, is five times as great as when turned towards the moon.

